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# NUMERACY & STATISTICS

March 2022

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## Time allowed

Three hours

## Instructions

- Ensure that you pay particular attention to words in **bold**.
- Write the question number next to each answer in your answer booklet.
- You are **not** required to rewrite the question in your answer booklet.
- Show all your workings.

## Information

- Different questions may carry a different number of marks.
- Marks for each question are shown in [ ].
- Questions start on page 4.

## Advice

- Read each question carefully before you start to answer it.
- Use the full time permitted and check all your answers.

## Materials

- Notes or books are **not** permitted.
- Non-programmable calculators are permitted.

## FORMULA SHEET

### Quadratic Formula

For a quadratic equation in the form  $ax^2 + bx + c = 0$ :

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

### Normal Distribution

The z score for a normal distribution:

$$z = \frac{x - \mu}{\sigma}$$

**STANDARD NORMAL DISTRIBUTION: Table Values Represent AREA to the LEFT of the Z score.**

**Table of the standard normal distribution values ( $z \leq 0$ )**

<b>z</b>	<b>0.00</b>	<b>0.01</b>	<b>0.02</b>	<b>0.03</b>	<b>0.04</b>	<b>0.05</b>	<b>0.06</b>	<b>0.07</b>	<b>0.08</b>	<b>0.09</b>
-0.0	0.50000	0.49601	0.49202	0.48803	0.48405	0.48006	0.47608	0.47210	0.46812	0.46414
-0.1	0.46017	0.45621	0.45224	0.44828	0.44433	0.44038	0.43644	0.43251	0.42858	0.42466
-0.2	0.42074	0.41683	0.41294	0.40905	0.40517	0.40129	0.39743	0.39358	0.38974	0.38591
-0.3	0.38209	0.37828	0.37448	0.37070	0.36693	0.36317	0.35942	0.35569	0.35197	0.34827
-0.4	0.34458	0.34090	0.33724	0.33360	0.32997	0.32636	0.32276	0.31918	0.31561	0.31207
-0.5	0.30854	0.30503	0.30153	0.29806	0.29460	0.29116	0.28774	0.28434	0.28096	0.27760
-0.6	0.27425	0.27093	0.26763	0.26435	0.26109	0.25785	0.25463	0.25143	0.24825	0.24510
-0.7	0.24196	0.23885	0.23576	0.23270	0.22965	0.22663	0.22363	0.22065	0.21770	0.21476
-0.8	0.21186	0.20897	0.20611	0.20327	0.20045	0.19766	0.19489	0.19215	0.18943	0.18673
-0.9	0.18406	0.18141	0.17879	0.17619	0.17361	0.17106	0.16853	0.16602	0.16354	0.16109
-1.0	0.15866	0.15625	0.15386	0.15151	0.14917	0.14686	0.14457	0.14231	0.14007	0.13786
-1.1	0.13567	0.13350	0.13136	0.12924	0.12714	0.12507	0.12302	0.12100	0.11900	0.11702
-1.2	0.11507	0.11314	0.11123	0.10935	0.10749	0.10565	0.10384	0.10204	0.10027	0.09853
-1.3	0.09680	0.09510	0.09342	0.09176	0.09012	0.08851	0.08692	0.08534	0.08379	0.08226
-1.4	0.08076	0.07927	0.07780	0.07636	0.07493	0.07353	0.07215	0.07078	0.06944	0.06811
-1.5	0.06681	0.06552	0.06426	0.06301	0.06178	0.06057	0.05938	0.05821	0.05705	0.05592
-1.6	0.05480	0.05370	0.05262	0.05155	0.05050	0.04947	0.04846	0.04746	0.04648	0.04551
-1.7	0.04457	0.04363	0.04272	0.04182	0.04093	0.04006	0.03920	0.03836	0.03754	0.03673
-1.8	0.03593	0.03515	0.03438	0.03363	0.03288	0.03216	0.03144	0.03074	0.03005	0.02938
-1.9	0.02872	0.02807	0.02743	0.02680	0.02619	0.02559	0.02500	0.02442	0.02385	0.02330
-2.0	0.02275	0.02222	0.02169	0.02118	0.02068	0.02018	0.01970	0.01923	0.01876	0.01831
-2.1	0.01786	0.01743	0.01700	0.01659	0.01618	0.01578	0.01539	0.01500	0.01463	0.01426
-2.2	0.01390	0.01355	0.01321	0.01287	0.01255	0.01222	0.01191	0.01160	0.01130	0.01101
-2.3	0.01072	0.01044	0.01017	0.00990	0.00964	0.00939	0.00914	0.00889	0.00866	0.00842
-2.4	0.00820	0.00798	0.00776	0.00755	0.00734	0.00714	0.00695	0.00676	0.00657	0.00639
-2.5	0.00621	0.00604	0.00587	0.00570	0.00554	0.00539	0.00523	0.00509	0.00494	0.00480
-2.6	0.00466	0.00453	0.00440	0.00427	0.00415	0.00403	0.00391	0.00379	0.00368	0.00357
-2.7	0.00347	0.00336	0.00326	0.00317	0.00307	0.00298	0.00289	0.00280	0.00272	0.00264
-2.8	0.00256	0.00248	0.00240	0.00233	0.00226	0.00219	0.00212	0.00205	0.00199	0.00193
-2.9	0.00187	0.00181	0.00175	0.00170	0.00164	0.00159	0.00154	0.00149	0.00144	0.00140
-3.0	0.00135	0.00131	0.00126	0.00122	0.00118	0.00114	0.00111	0.00107	0.00104	0.00100
-3.1	0.00097	0.00094	0.00090	0.00087	0.00085	0.00082	0.00079	0.00076	0.00074	0.00071
-3.2	0.00069	0.00066	0.00064	0.00062	0.00060	0.00058	0.00056	0.00054	0.00052	0.00050
-3.3	0.00048	0.00047	0.00045	0.00043	0.00042	0.00040	0.00039	0.00038	0.00036	0.00035
-3.4	0.00034	0.00033	0.00031	0.00030	0.00029	0.00028	0.00027	0.00026	0.00025	0.00024
-3.5	0.00023	0.00022	0.00022	0.00021	0.00020	0.00019	0.00019	0.00018	0.00017	0.00017

**Table of the standard normal distribution values ( $z \geq 0$ )**

<b>z</b>	<b>0.00</b>	<b>0.01</b>	<b>0.02</b>	<b>0.03</b>	<b>0.04</b>	<b>0.05</b>	<b>0.06</b>	<b>0.07</b>	<b>0.08</b>	<b>0.09</b>
<b>0.0</b>	0.50000	0.50399	0.50798	0.51197	0.51595	0.51994	0.52392	0.52790	0.53188	0.53586
<b>0.1</b>	0.53983	0.54380	0.54776	0.55172	0.55567	0.55962	0.56356	0.56749	0.57142	0.57535
<b>0.2</b>	0.57926	0.58317	0.58706	0.59095	0.59483	0.59871	0.60257	0.60642	0.61026	0.61409
<b>0.3</b>	0.61791	0.62172	0.62552	0.62930	0.63307	0.63683	0.64058	0.64431	0.64803	0.65173
<b>0.4</b>	0.65542	0.65910	0.66276	0.66640	0.67003	0.67364	0.67724	0.68082	0.68439	0.68793
<b>0.5</b>	0.69146	0.69497	0.69847	0.70194	0.70540	0.70884	0.71226	0.71566	0.71904	0.72240
<b>0.6</b>	0.72575	0.72907	0.73237	0.73565	0.73891	0.74215	0.74537	0.74857	0.75175	0.75490
<b>0.7</b>	0.75804	0.76115	0.76424	0.76730	0.77035	0.77337	0.77637	0.77935	0.78230	0.78524
<b>0.8</b>	0.78814	0.79103	0.79389	0.79673	0.79955	0.80234	0.80511	0.80785	0.81057	0.81327
<b>0.9</b>	0.81594	0.81859	0.82121	0.82381	0.82639	0.82894	0.83147	0.83398	0.83646	0.83891
<b>1.0</b>	0.84134	0.84375	0.84614	0.84849	0.85083	0.85314	0.85543	0.85769	0.85993	0.86214
<b>1.1</b>	0.86433	0.86650	0.86864	0.87076	0.87286	0.87493	0.87698	0.87900	0.88100	0.88298
<b>1.2</b>	0.88493	0.88686	0.88877	0.89065	0.89251	0.89435	0.89617	0.89796	0.89973	0.90147
<b>1.3</b>	0.90320	0.90490	0.90658	0.90824	0.90988	0.91149	0.91308	0.91466	0.91621	0.91774
<b>1.4</b>	0.91924	0.92073	0.92220	0.92364	0.92507	0.92647	0.92785	0.92922	0.93056	0.93189
<b>1.5</b>	0.93319	0.93448	0.93574	0.93699	0.93822	0.93943	0.94062	0.94179	0.94295	0.94408
<b>1.6</b>	0.94520	0.94630	0.94738	0.94845	0.94950	0.95053	0.95154	0.95254	0.95352	0.95449
<b>1.7</b>	0.95543	0.95637	0.95728	0.95818	0.95907	0.95994	0.96080	0.96164	0.96246	0.96327
<b>1.8</b>	0.96407	0.96485	0.96562	0.96638	0.96712	0.96784	0.96856	0.96926	0.96995	0.97062
<b>1.9</b>	0.97128	0.97193	0.97257	0.97320	0.97381	0.97441	0.97500	0.97558	0.97615	0.97670
<b>2.0</b>	0.97725	0.97778	0.97831	0.97882	0.97932	0.97982	0.98030	0.98077	0.98124	0.98169
<b>2.1</b>	0.98214	0.98257	0.98300	0.98341	0.98382	0.98422	0.98461	0.98500	0.98537	0.98574
<b>2.2</b>	0.98610	0.98645	0.98679	0.98713	0.98745	0.98778	0.98809	0.98840	0.98870	0.98899
<b>2.3</b>	0.98928	0.98956	0.98983	0.99010	0.99036	0.99061	0.99086	0.99111	0.99134	0.99158
<b>2.4</b>	0.99180	0.99202	0.99224	0.99245	0.99266	0.99286	0.99305	0.99324	0.99343	0.99361
<b>2.5</b>	0.99379	0.99396	0.99413	0.99430	0.99446	0.99461	0.99477	0.99492	0.99506	0.99520
<b>2.6</b>	0.99534	0.99547	0.99560	0.99573	0.99585	0.99598	0.99609	0.99621	0.99632	0.99643
<b>2.7</b>	0.99653	0.99664	0.99674	0.99683	0.99693	0.99702	0.99711	0.99720	0.99728	0.99736
<b>2.8</b>	0.99744	0.99752	0.99760	0.99767	0.99774	0.99781	0.99788	0.99795	0.99801	0.99807
<b>2.9</b>	0.99813	0.99819	0.99825	0.99831	0.99836	0.99841	0.99846	0.99851	0.99856	0.99861
<b>3.0</b>	0.99865	0.99869	0.99874	0.99878	0.99882	0.99886	0.99889	0.99893	0.99896	0.99900
<b>3.1</b>	0.99903	0.99906	0.99910	0.99913	0.99916	0.99918	0.99921	0.99924	0.99926	0.99929
<b>3.2</b>	0.99931	0.99934	0.99936	0.99938	0.99940	0.99942	0.99944	0.99946	0.99948	0.99950
<b>3.3</b>	0.99952	0.99953	0.99955	0.99957	0.99958	0.99960	0.99961	0.99962	0.99964	0.99965
<b>3.4</b>	0.99966	0.99968	0.99969	0.99970	0.99971	0.99972	0.99973	0.99974	0.99975	0.99976
<b>3.5</b>	0.99977	0.99978	0.99978	0.99979	0.99980	0.99981	0.99981	0.99982	0.99983	0.99983

**ANSWER SEVEN QUESTIONS IN TOTAL**  
**ANSWER ALL QUESTIONS FROM SECTION A**  
**ANSWER ANY THREE QUESTIONS FROM SECTION B**

**SECTION A (ANSWER ALL QUESTIONS)**

1. Calculate each of the following:

(a)  $7^4 - 3^2$

[3 marks]

(b)  $8^0 + 8^1$

[2 marks]

2. (a) Express the following as a single fraction:

$$\frac{5}{8} - \frac{53-13}{48}$$

[3 marks]

(b) Calculate the following to **three** decimal places:

14% of \$32.53

[3 marks]

(c) Kate's salary is £40,000 per annum following an increase of 3% per annum.

Calculate Kate's salary per annum before the increase. Give your answer to the nearest whole £.

[4 marks]

3. Hot and cold food is sold at a café. The following data has recorded the sales of hot food over a ten day period including the temperature outside the café:

**Sales of hot food compared with temperatures**

Sales (\$'00)	Temperature °C
6	20
6.5	23
7.2	25
1	32
5	28
10	17
8	18
2	30
2.5	25
5	25

(a) Draw a graph plotting the data as a scatter diagram, including a line of best fit.

[10 marks]

(b) Estimate the amount of hot food sales when the temperature is 21°C using the line of best fit.

[3 marks]

(c) State the difference between quantitative and qualitative data.

[2 marks]

4. A retailer has been analysing the sales of five departments. The overall sales were £800,000. The following shows the % of overall sales that each department contributed to overall sales last month:

Department sales	
Department	% of overall sales
Baby and Child	10
Homeware	4
Clothing	27
Electronic	42
Fashion	17

Draw a bar chart and plot the actual sales per department (not the % of overall sales) for the data provided.

[10 marks]

### SECTION B (ANSWER ANY THREE QUESTIONS)

5. A bank is advertising a new savings account. It is an account that will last for eight years. The annual rate of interest is 1.25% for the first three years. It increases to 1.67% for the next three years. For the final two years it increases to 3.08%.

- (a) Harry deposits \$8,500 into the account and never withdraws from it.

Calculate the amount that will be in Harry's account after:

(i) Two years

[3 marks]

(ii) Five years

[5 marks]

(iii) Eight years

[4 marks]

- (b) Kate also deposited \$5,750 into an account. Interest is paid annually and there is no penalty for withdrawing any money. Interest is calculated annually and based on is the amount in the account on 1<sup>st</sup> April each year.

- (i) Kate withdraws \$1,000 on 2<sup>nd</sup> April after the end of year three.

Calculate the amount that will be in Kate's account at the end of year four.

[4 marks]

- (ii) Kate withdraws \$2,500 on 2<sup>nd</sup> April after the end of year four and then does not withdraw any more money from the account.

Calculate the amount that will be in Kate's account at the end of year eight.

[4 marks]

6. (a) Solve the following simultaneous equations using the algebraic approach:

$$y = 4x + 26$$

$$3y = x + 100$$

[8 marks]

- (b) Draw a graph and plot the following non-linear equation showing when  $x = -2, -1, 0, +1$  and  $+2$ :

$$y = 3x^3 + x^2 - 4x - 7$$

[12 marks]

7. The distribution of sales in a shoe shop is normally distributed. The mean monthly sales is £76,250 with a standard deviation of £6,500.

- (a) Calculate the proportion of time that monthly sales are less than £70,000. Give your answer to **three** decimal places.

[6 marks]

- (b) Calculate the proportion of time that monthly sales are between £74,000 and £84,000. Give your answer to **two** decimal places.

[11 marks]

- (c) Draw a normal distribution curve for the monthly sales of shoes, labelling the mean and **one** standard deviation either side of the mean.

[3 marks]

8. (a) An investor is deciding whether to invest in a business opportunity. The table below shows the only four potential outcomes. The probability of making a profit of €8,000 is 15%. The probability of making a loss of €1,000 is one-quarter. The probability of making a loss of €2,000 is  $\frac{1}{5}$ .

**Potential outcomes**

Profit of €8,000
Profit of €2,000
Loss of €1,000
Loss of €2,000

- (i) Calculate the expected value of profit or loss for this investment. [7 marks]
- (ii) Suggest whether the investor should invest in the business opportunity including reasons for your suggestion. [3 marks]

- (b) The estimated daily sales of a new designer jacket are as follows:

**Estimated daily sales**

Number of jackets sold	Probability
1,000	0.66
1,250	0.14
1,500	0.08
2,000	0.12

To make a profit there needs to be an expected daily sale of 1,300 jackets.

- Explain whether a profit will be made based on the expected daily sales. [5 marks]
- (c) William, Kate and Harry have all invested in a new company. William invested £25,000, Kate invested £10,000 and Harry invested £15,000. Any gross profits are divided in the same ratio as their investments.
- (i) State William, Kate and Harry's investment as a ratio in its simplest form. [2 marks]
- (ii) At the end of year one, the company generated a gross profit of £16,255. Calculate the gross amount that Harry will receive. [3 marks]

**END OF QUESTIONS**